

# Fully Automated Shape Analysis Based on Forest Automata<sup>†</sup>

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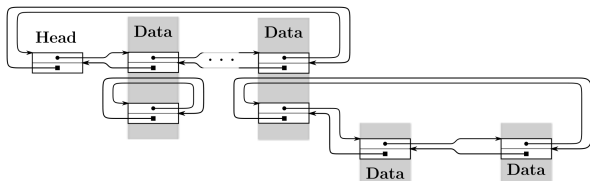
<sup>†</sup>To appear in *Proc. of CAV'13*.



# Shape Analysis

## ■ Precise **shape analysis**:

- ▶ a notoriously difficult problem



- ▶ specialized solutions (lists)
- ▶ help from the outside (loop invariants, inductive predicates)

## ■ Classes of errors:

- ▶ **error line** reachability
- ▶ **invalid pointer** dereference
- ▶ occurrence of **garbage**

## ■ Separation Logic

- ☺ local reasoning, well scalable
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## ■ Abstract Regular Tree Model Checking (ARTMC)

- ☺ uses tree automata (TA), flexible and refinable abstraction
- ☹ monolithic encoding of the heap, not very scalable

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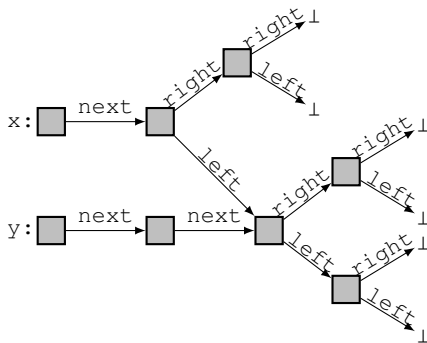
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  - splitting the heap into tree componentsand
  - representing sets of heaps using TA

# Heap Representation

- Forest decomposition of a heap

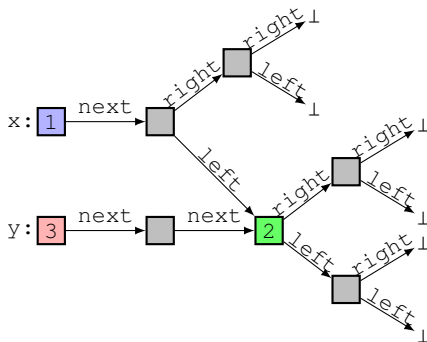


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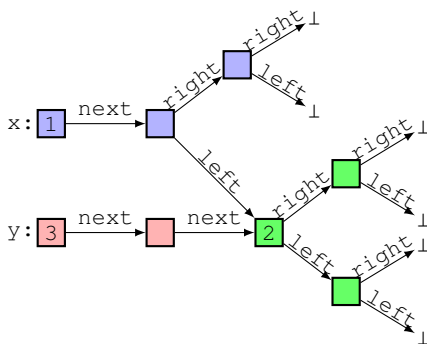


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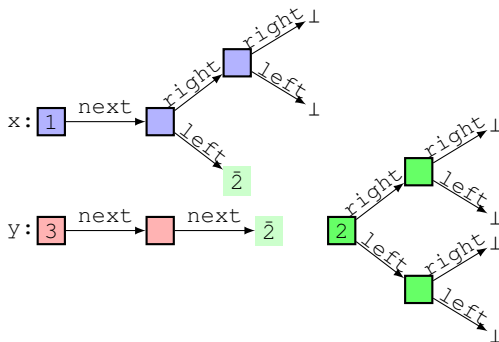


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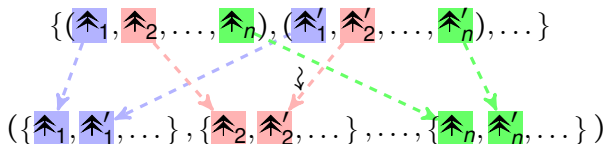
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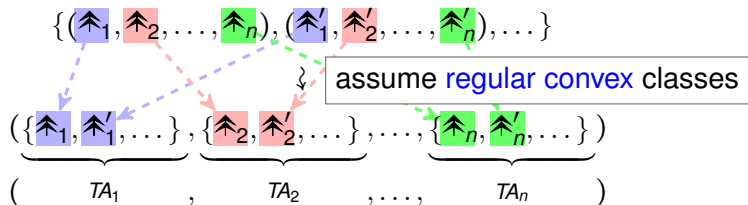
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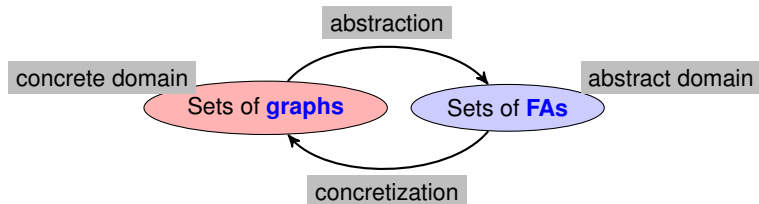
**Forest Automaton**

assume **regular convex** classes

$$(\{\uparrow_1, \uparrow'_1, \dots\}, \{\uparrow_2, \uparrow'_2, \dots\}, \dots, \{\uparrow_n, \uparrow'_n, \dots\})$$

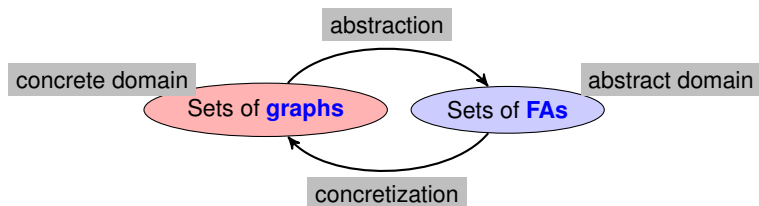
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# Symbolic Execution

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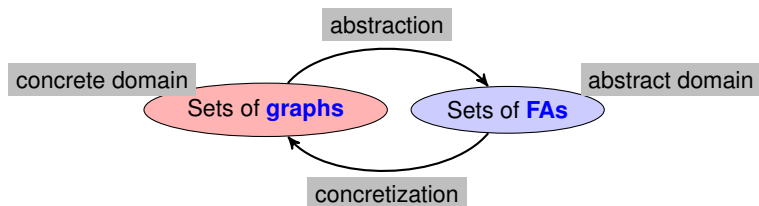


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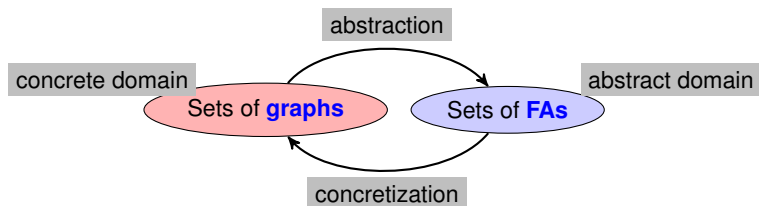
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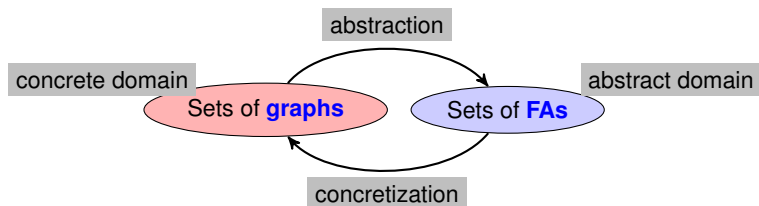
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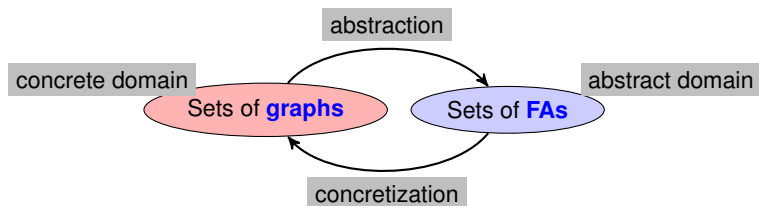
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append a TA

remove a TA

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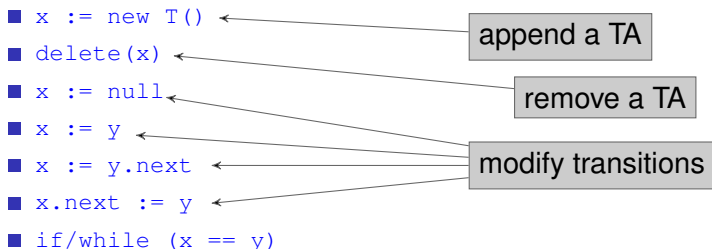
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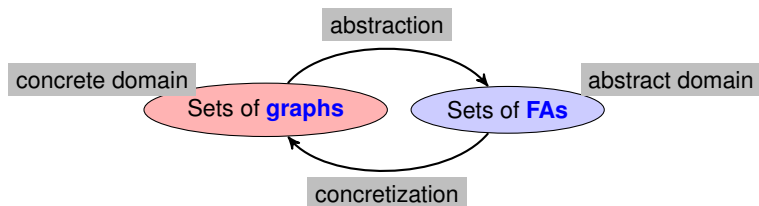
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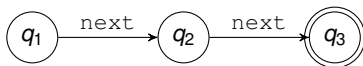
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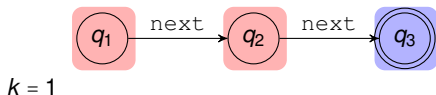
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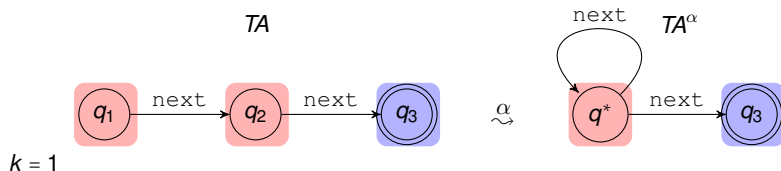
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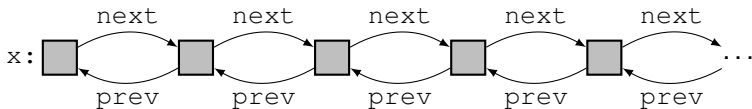
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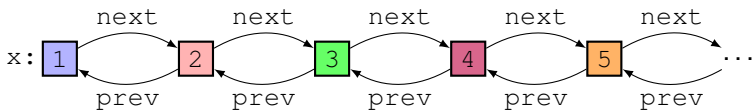


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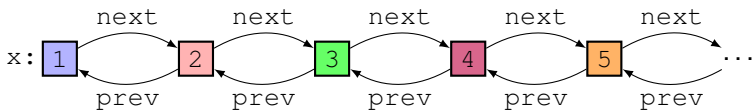


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- doubly linked lists (DLLs), circular lists, nested lists,
- trees with parent pointers,
- skip lists

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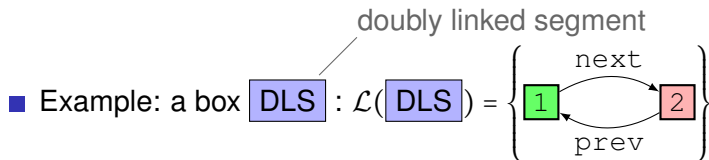
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- Example: a box DLS doubly linked segment

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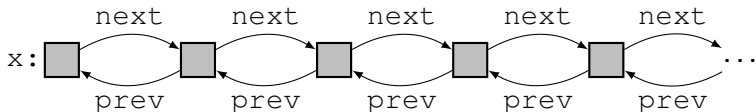
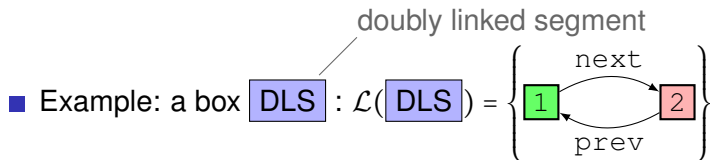




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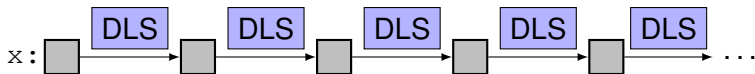
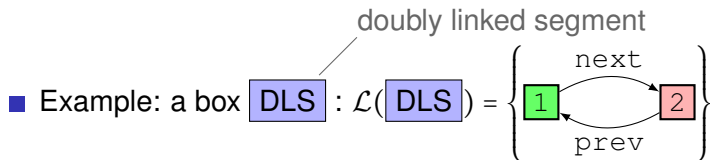
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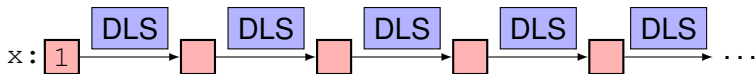
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■ Example: a box **DLS** :  $\mathcal{L}(\text{DLS}) = \left\{ \begin{array}{c} \text{next} \\ \text{1} \rightleftarrows \text{2} \\ \text{prev} \end{array} \right\}$

doubly linked segment



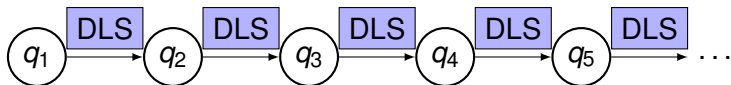
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■ Example: a box **DLS** :  $\mathcal{L}(\text{DLS}) = \left\{ \begin{array}{c} \text{next} \\ \text{1} \rightleftarrows \text{2} \\ \text{prev} \end{array} \right\}$

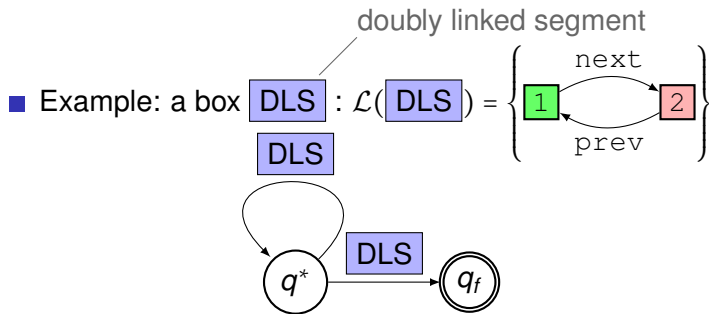
doubly linked segment



# Hierarchical Forest Automata

## ■ Hierarchical Forest Automata

- ▶ FAs are **symbols (boxes)** of FAs of a **higher level**
- ▶ a **hierarchy** of FAs
- ▶ Intuition: replace **repeated subgraphs** with a **single symbol**



## The Challenge

How to find “**the right**” boxes?

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- CAV'11 — **database** of boxes
- CAV'13 — **automatic discovery**

# Learning of Boxes

- compromise between

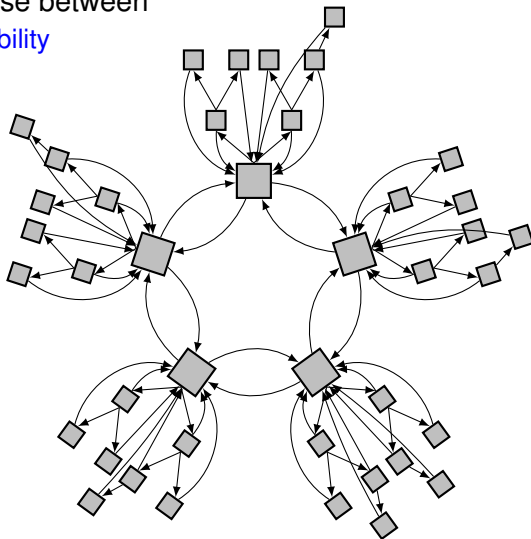


# Learning of Boxes

- compromise between
  - [reusability](#)

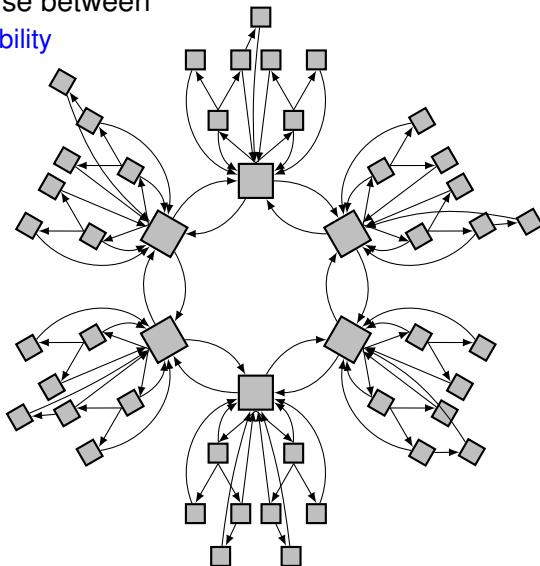
# Learning of Boxes

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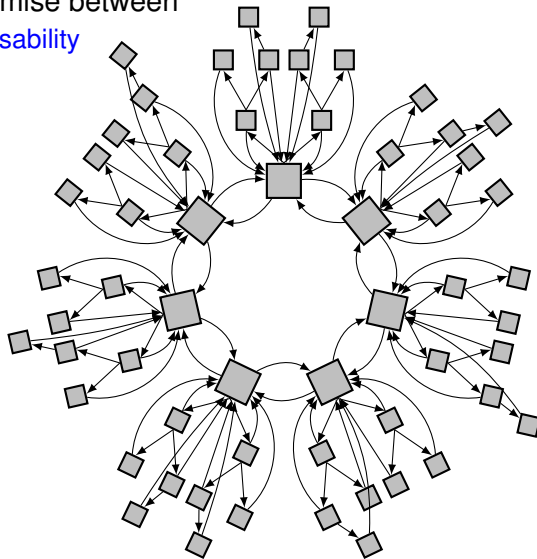
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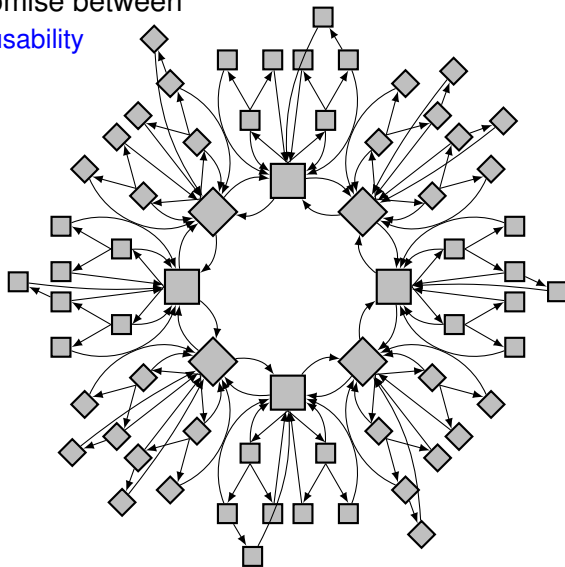
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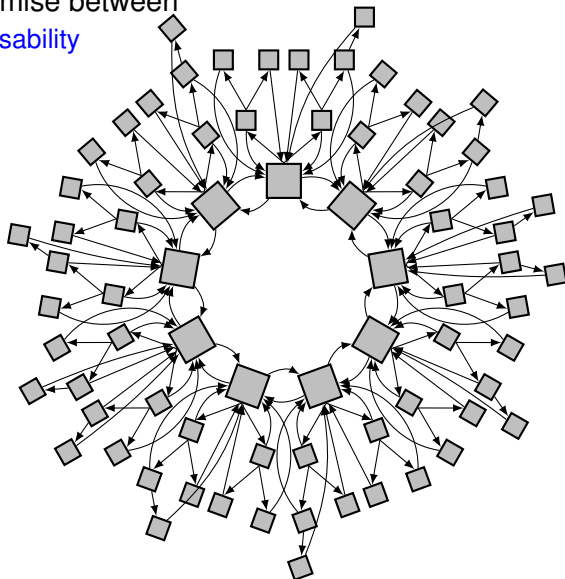
# Learning of Boxes

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# Learning of Boxes

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# Learning of Boxes

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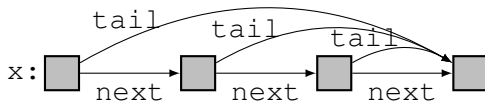
# Learning of Boxes

- compromise between
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  - ability to hide cut-points



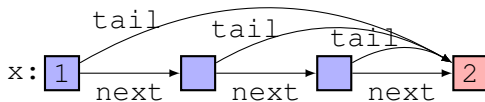
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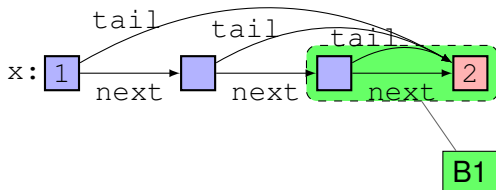
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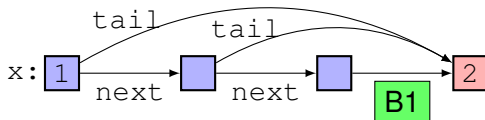
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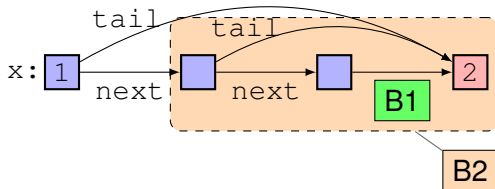
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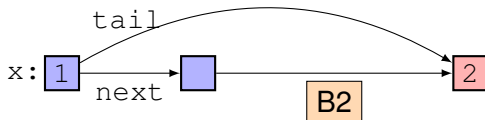
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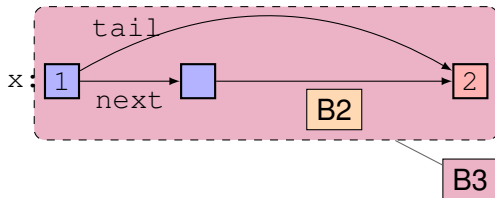
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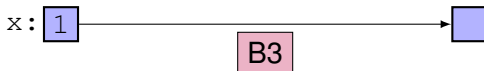
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# Learning of Boxes

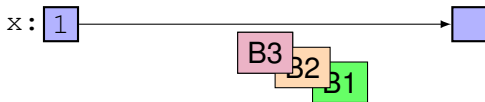
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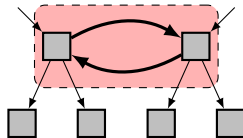
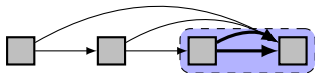
# Learning of Boxes: Knots

## Knots

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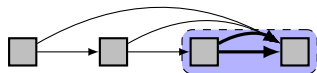
- 1 smallest subgraphs meaningful to be folded:



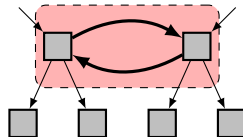
# Learning of Boxes: Knots

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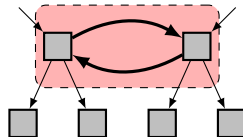
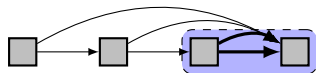
- 2 handle inputs/outputs



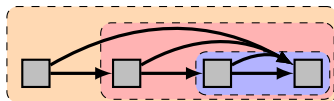
# Learning of Boxes: Knots

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# Learning of Boxes: Knots

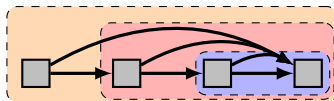
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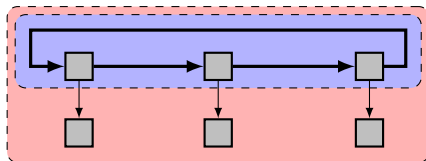


- 2 handle inputs/outputs

- ▶ **join** intersecting knots

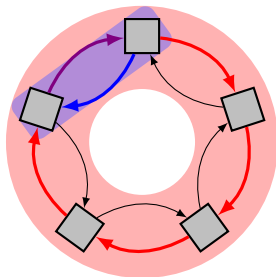


- ▶ **enclose** paths from inner nodes to leaves



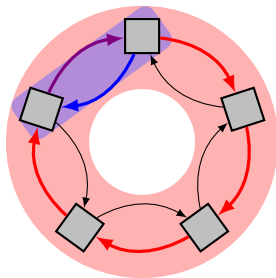
## 3 complexity

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- ▶ find basic knots with  $1, 2, \dots$  cut-points

# Widening Revisited

- **learning** and **folding** of boxes in the abstraction loop

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## The Goal

Fold boxes that will, after abstraction, appear on cycles of automata.

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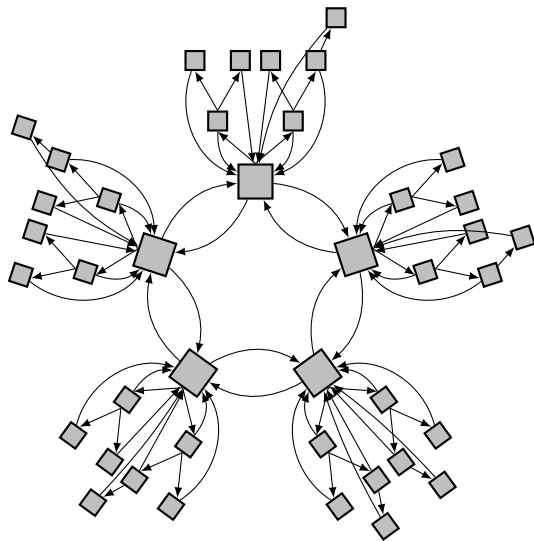
Fold boxes that will, after abstraction, appear on cycles of automata.

⇒ hide unboundedly many cut-points

- 1 **Algorithm:** Abstraction Loop
- 2 *Unfold solo boxes*
- 3 **repeat**
- 4     *Abstract*
- 5     *Fold*
- 6 **until** *fixpoint*

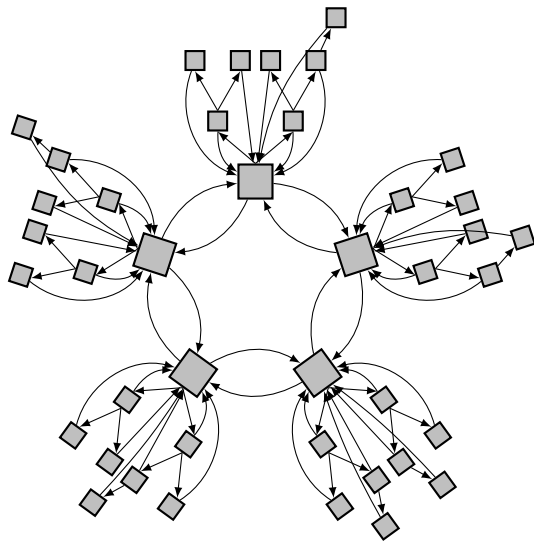
not on a cycle

# Learning of Boxes: Example



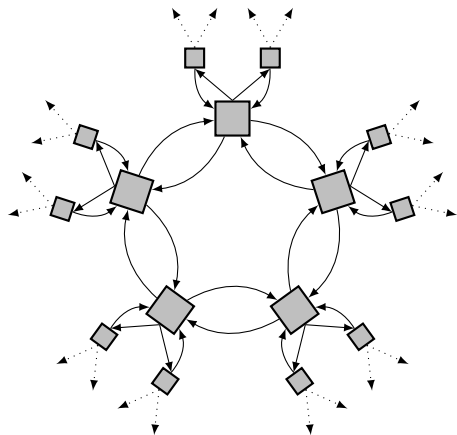
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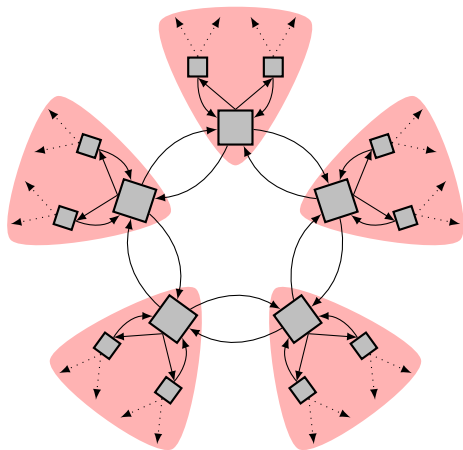
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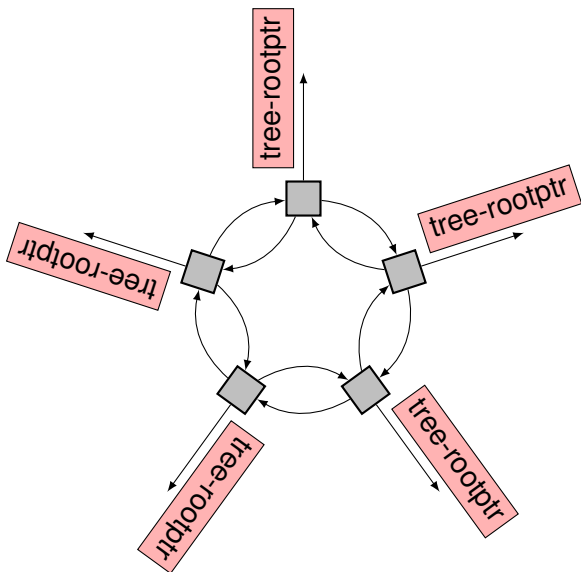
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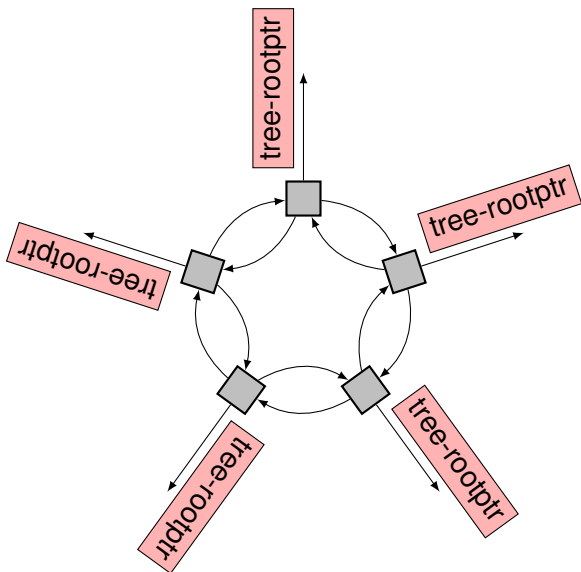


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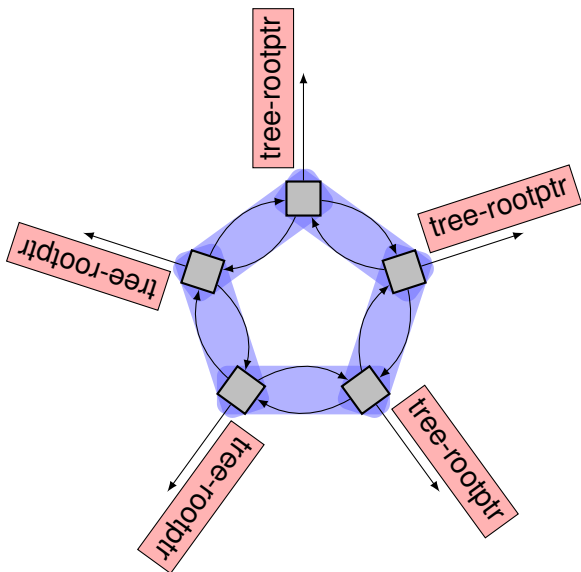
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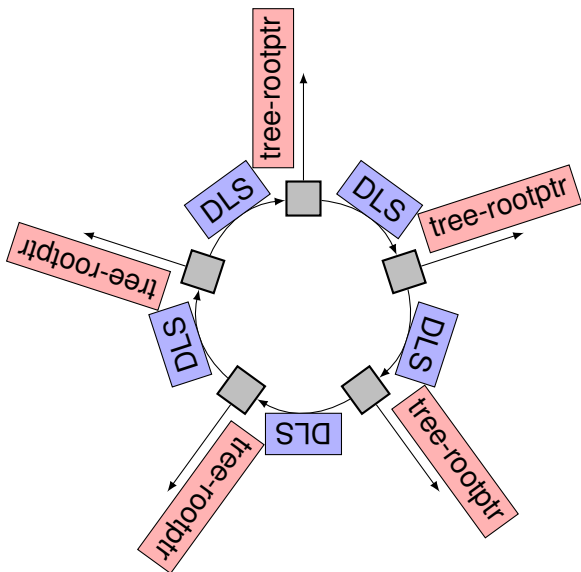
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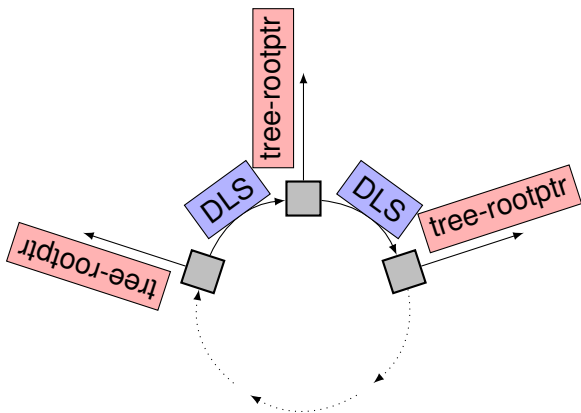
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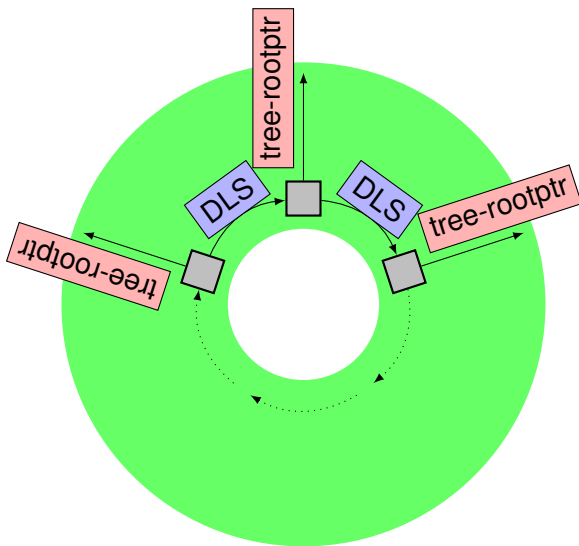
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# Learning of Boxes: Example

circular-DLL-of  
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# Experimental Results

- implemented in **Forester** tool



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Table : Results of the experiments [s]

Example	FA	Predator	Example	FA	Predator
SLL (delete)	0.04	0.04	DLL (reverse)	0.06	0.03
SLL (bubblesort)	0.04	0.03	DLL (insert)	0.07	0.05
SLL (mergesort)	0.15	0.10	DLL (insertsort <sub>1</sub> )	0.40	0.11
SLL (insertsort)	0.05	0.04	DLL (insertsort <sub>2</sub> )	0.12	0.05
SLL (reverse)	0.03	0.03	DLL of CDLLs	1.25	0.22
SLL+head	0.05	0.03	DLL+subdata	0.09	T
SLL of 0/1 SLLs	0.03	0.11	CDLL	0.03	0.03
SLL <sub>Linux</sub>	0.03	0.03	tree	0.14	Err
SLL of CSLLs	0.73	0.12	tree+parents	0.21	T
SLL of 2CDLLs <sub>Linux</sub>	0.17	0.25	tree+stack	0.08	Err
skip list <sub>2</sub>	0.42	T	tree (DSW) <sup>Deutsch-Schorr-Waite</sup>	0.40	Err
skip list <sub>3</sub>	9.14	T	tree of CSLLs	0.42	Err

timeout

false positive

# Conclusion

Shape analysis with [forest automata](#):

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Shape analysis with **forest automata**:

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  - **skip lists**
- not covered here:
  - support for **pointer arithmetic**
  - tracking **ordering** relations
    - P. Abdulla, L. Holík, B. Jonsson, O. Lengál, C.Q. Tring, and T. Vojnar. **Verification of Heap Manipulating Programs with Ordered Data by Extended Forest Automata**. To appear in *Proc. of ATVA'13*.



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- **recursive** boxes
  - B+ trees, ...